

Motion in a Plane

Question1

Two bodies are projected from the same point with the same initial velocity ' u ' making angles ' θ ' and ' $(90^\circ - \theta)$ ' with the horizontal in opposite directions. The horizontal distance between their positions when the bodies are at their maximum heights is

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Options:

A.

$$\frac{u^2}{2g} (\sin^2 \theta - \cos^2 \theta)$$

B.

$$\frac{u^2 \sin 2\theta}{2g}$$

C.

$$\frac{u^2}{g}$$

D.

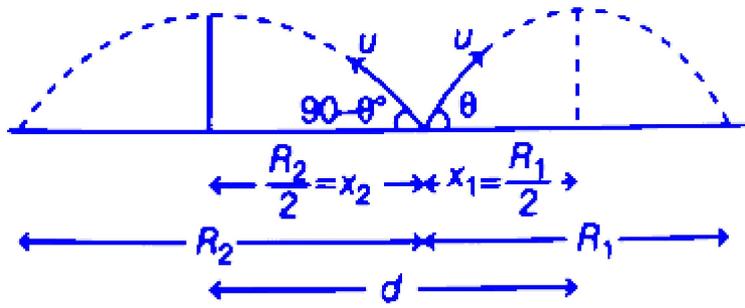
$$\frac{u^2 \sin 2(90^\circ - \theta)}{g}$$

Answer: D

Solution:

The given situation is shown below in figure.





$$x_1 = \frac{R_1}{2} = \frac{u^2 \sin 2\theta}{2g}$$

$$\text{and } x_2 = \frac{R_2}{2} = \frac{u^2 \sin 2(90^\circ - \theta)}{2g}$$

$$\therefore = \frac{u^2 \sin(180^\circ - 2\theta)}{2g} = \frac{u^2 \sin 2\theta}{2g}$$

$$\therefore d = x_1 + x_2$$

$$= \frac{u^2 \sin 2\theta}{2g} + \frac{u^2 \sin 2\theta}{2g} = \frac{u^2 \sin 2\theta}{g}$$

$$= \frac{u^2 \sin(180^\circ - 2\theta)}{g} = \frac{u^2 \sin 2(90^\circ - \theta)}{g}$$

Question2

A helicopter flying horizontally with a velocity of 288 km/h drops a bomb. If the line joining the point of dropping the bomb and the point where bomb hits the ground makes an angle 45° with the horizontal, then the height at which the bomb was dropped is (Acceleration due to gravity = 10 ms^{-2})

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Options:

A.

1320 m

B.

1280 m

C.

320 m

D.

640 m

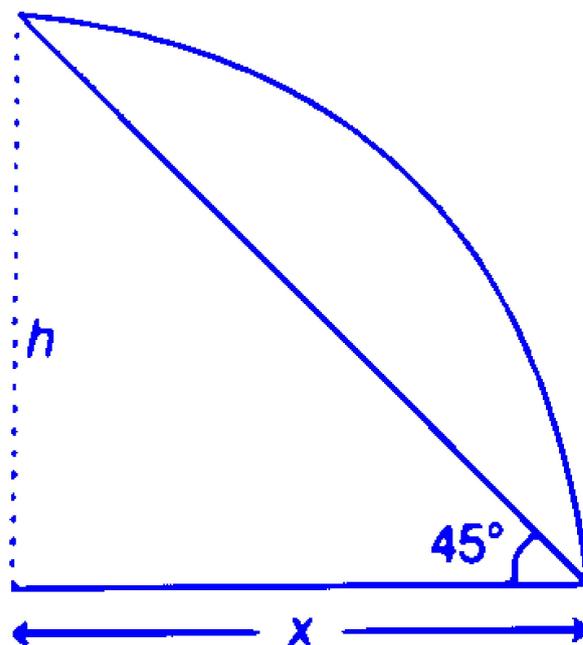
Answer: B

Solution:

$$u = 288 \text{ km/h}$$
$$= 288 \times \frac{5}{18} = 80 \text{ m/s}$$

$$h = \frac{1}{2}gt^2$$

$$x = ut$$



$$\therefore \tan 45^\circ = \frac{h}{x}$$

$$\Rightarrow h = x \Rightarrow \frac{1}{2}gt^2 = ut$$

$$\Rightarrow t = \frac{2u}{g} = \frac{2 \times 80}{10} \Rightarrow t = 16 \text{ s}$$

$$\therefore \text{Height of bomb, } h = \frac{1}{2}gt^2$$

$$= \frac{1}{2} \times 10 \times 16^2 = 1280 \text{ m}$$

Question3

The maximum horizontal range of a ball projected from the ground is 32 m . If the ball is thrown with the same speed horizontally from the top of a tower of . height 25 m , the maximum horizontal distance covered by the ball is

(Acceleration due to gravity = 10 ms^{-2})

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Options:

A. 40 m

B. 57 m

C. 60 m

D. 75 m

Answer: A

Solution:

The maximum horizontal range (R) of a projectile launched at an optimal angle (45°) is given by,

$$R = \frac{u^2 \sin 2\theta}{g}$$

Given, $R = 32 \text{ m}$

$$\text{Then } 32 = \frac{u^2 \cdot \sin 2 \cdot 45^\circ}{10}$$

$$u^2 = 320$$

$$u = 8\sqrt{5} \text{ m/s}$$

When the ball is thrown horizontally from the top of a tower of height 25 m , the vertical motion is given by,

$$y = \frac{1}{2}gt^2$$

Given, $y = 25 \text{ m}$

$$\text{Then, } 25 = \frac{1}{2} \times 10 \times t^2$$

$$t = \sqrt{5} \text{ s}$$

The horizontal distance x covered by the ball is given by,



$$x = ut$$

From Eqs. (i) and (ii), we get

$$x = 8\sqrt{5} \times \sqrt{5}$$

$$x = 8 \times 5$$

$$x = 40 \text{ m}$$

Question4

From a height of h above the ground, a ball is projected up at an angle 30° with the horizontal. If the ball strikes the ground with a speed of 1.25 times its initial speed of 40 ms^{-1} , the value of h is (acceleration due to gravity = 10 ms^{-2})

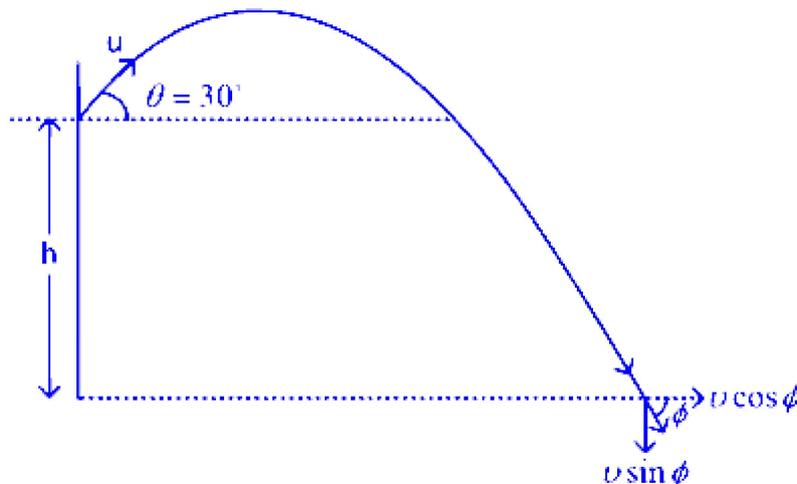
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Options:

- A. 75 m
- B. 60 m
- C. 30 m
- D. 45 m

Answer: D

Solution:



Initial speed, $u = 40 \text{ m/s}$

Final speed, $v = 1.25 \times u$

$v = 50 \text{ m/s}$

\therefore Horizontal component is constant

$$\Rightarrow 40 \times \frac{\sqrt{3}}{2} = 50 \cos \phi$$

$$\Rightarrow \cos \phi = \frac{4\sqrt{3}}{10}$$

Vertical component

$$v_y = v \sin \phi = v \sqrt{1 - \cos^2 \phi}$$

$$v_y = 50 \sqrt{1 - \left(\frac{4\sqrt{3}}{10}\right)^2}$$

$$= 5\sqrt{52}$$

Now using 3rd equation of motion

$$\Rightarrow (5\sqrt{52})^2 - (40 \sin 30^\circ)^2 = 2gh$$

$$\Rightarrow h = \frac{1300 - 400}{2 \times 10} = 45 \text{ m}$$

$$h = 45 \text{ m}$$

Question5

A body is projected from the ground at an angle of $\tan^{-1}(\sqrt{7})$ with the horizontal. At half of the maximum height, the speed of the body is n times the speed of projection. The value of n is

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Options:

A. 2

B. $\frac{1}{2}$

C. $\frac{4}{3}$

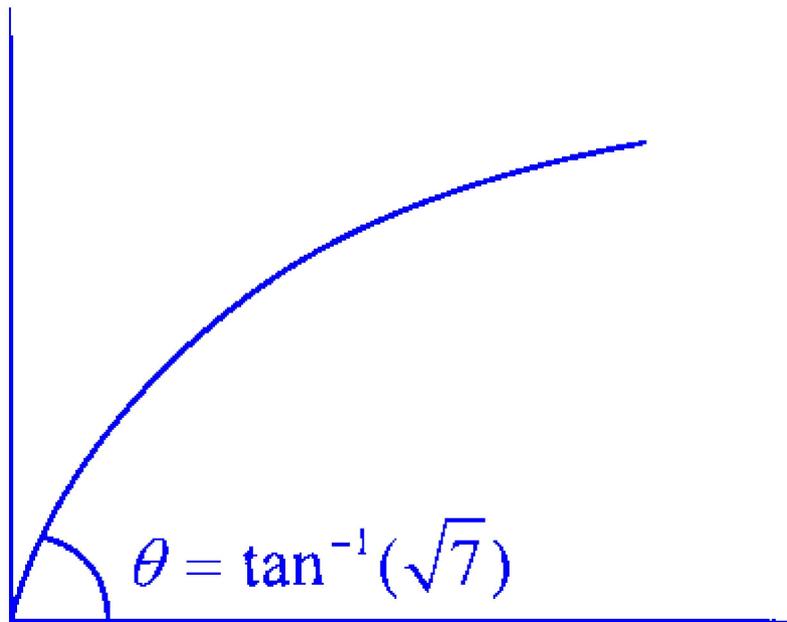


D. $\frac{3}{4}$

Answer: D

Solution:

Given,



$$\theta = \tan^{-1}(\sqrt{7})$$

Maximum height

$$H_{\max} = \frac{u^2 \sin^2 \theta}{2g}$$

[Put $\theta = \tan^{-1}(\sqrt{7})$]

$$H_{\max} = \frac{7}{8} \frac{u^2}{2g}$$

$$\frac{H_{\max}}{2} = \frac{7}{16} \frac{u^2}{2g}$$

Using 3rd equation of motion for velocity at $\frac{H_{\max}}{2}$

$$v^2 = u^2 - 2gh$$

where $v = nu$ (given)

$$h = \frac{H_{\max}}{2}$$

$$n^2 u^2 = u^2 - 2g \frac{H_{\max}}{2}$$

$$(n^2 - 1)u^2 = -2g \times \frac{7}{16} \frac{u^2}{2g}$$

$$n^2 - 1 = \frac{-7}{16} \Rightarrow n^2 = \frac{-7}{16} + 1$$

$$n^2 = \frac{9}{16}$$

$$n = \frac{3}{4}$$

Question6

A cannon placed on a cliff at a height of 375 m fires a cannon ball with a velocity of 100 ms^{-1} at an angle of 30° above the horizontal. The horizontal distance between the cannon and the target is (Acceleration due to gravity = 10 ms^{-2})

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Options:

A. $750\sqrt{3}$ m

B. $500\sqrt{3}$ m

C. $250\sqrt{3}$ m

D. 750 m

Answer: A

Solution:

Given, initial height, $y_i = 375$ m

Final height, $y_f = 0$ m

Initial velocity, $v_i = 100$ m/s



Initial horizontal range, $x_i = 0$

Angle of projection, $\theta = 30^\circ$

Now, $y_f = y_i + v_i t - \frac{1}{2}gt^2$

$$y_f = y_i + v_i g \sin \theta t - \frac{1}{2}gt^2$$

$$0 = 375 + (100 \times \sin 30^\circ)t - \frac{1}{2} \times 9.8t^2$$

$$0 = 375 + 50t - 4.9t^2$$

$$\Rightarrow 4.9t^2 - 50t - 375 = 0$$

On solving, we get

$$t_1 = 15.22 \text{ s and } t_2 = -5.02 \text{ s}$$

Now time cannot be negative hence,

$$t = 15.22 \text{ s}$$

Thus horizontal rang, $R = v_t \cos \theta t$

$$= 100 \times \cos 30^\circ \times 15.22$$

$$= 100 \times \frac{\sqrt{3}}{2} \times 15.22$$

$$= 761\sqrt{3} \text{ m} \approx 750\sqrt{3}$$

Question7

A body P is projected at an angle of 30° with the horizontal and another body Q is projected at an angle of 30° with the vertical. If the ratio of the horizontal ranges of the bodies P and Q is $1 : 2$, then the ratio of the maximum heights reached by the bodies P and Q is

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Options:

A. $1 : 4$

B. $1 : 6$

C. $2 : 3$



D. 1 : 1

Answer: B

Solution:

Given, $\theta_p = 30^\circ$ (Horizontal)

$\theta_Q = 30^\circ$ (Vertical)

$$= 90^\circ - 30^\circ = 60^\circ$$

thus, $\theta_Q = 60^\circ$ (Horizontal)

Maximum range reached,

$$R = \frac{v_0^2 \sin 2\theta}{g}$$

For body P ,

$$R_p = \frac{v_1^2 \sin 60^\circ}{g} \dots (i)$$

For body Q

$$R_Q = \frac{v_2^2 \sin 120^\circ}{g} \dots (ii)$$

The ratio of $\frac{R_P}{R_Q} = \frac{v_1^2}{v_2^2} = \frac{1}{2}$

$$\frac{H_P}{H_Q} = \frac{v_1^2}{v_2^2} \times \frac{\sin^2 30^\circ}{\sin^2 60^\circ}$$

$$= \frac{1}{2} \times \frac{1}{4} \times \frac{4}{3} = \frac{1}{6}$$

Question8

A person walks in such a way that he covers equal distance in each step. The person takes 2 steps forwards towards east, then takes a right turn and

walks 4 steps towards south, then takes a right turn and walks 6 steps towards west and then takes a right turn and walks further. The direction of his final position after a total of 20 steps walk with respect to his initial position is



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Options:

- A. North-West
- B. 60° West of South
- C. 60° South of West
- D. South-East

Answer: A

Solution:

Given,

Each step distance is equal.

1st \rightarrow 2 step towards east.

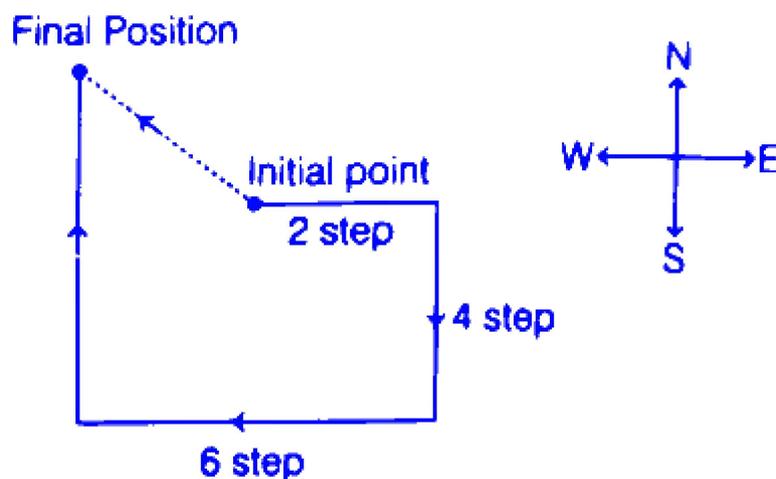
2nd \rightarrow take right and walks 4 steps south

3rd \rightarrow take right and walks 6 steps towards west.

4th \rightarrow take right and walks.

Total steps = 20.

Draw the given data,



At last turn, person travels

$$= 20 - 6 + 4 + 2 = 8 \text{ steps}$$

Thus, final direction is north west.

Question9

A bomb is dropped on an enemy post on the ground by an aeroplane flying horizontally with a velocity of 60kmh^{-1} at a height of 490 m . At the time of dropping the bomb, the horizontal distance of the aeroplane from the enemy post, so that the bomb hits the target is

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Options:

- A. $(\frac{400}{3})\text{m}$
- B. $(\frac{500}{3})\text{m}$
- C. $(\frac{1700}{3})\text{m}$
- D. 498 m

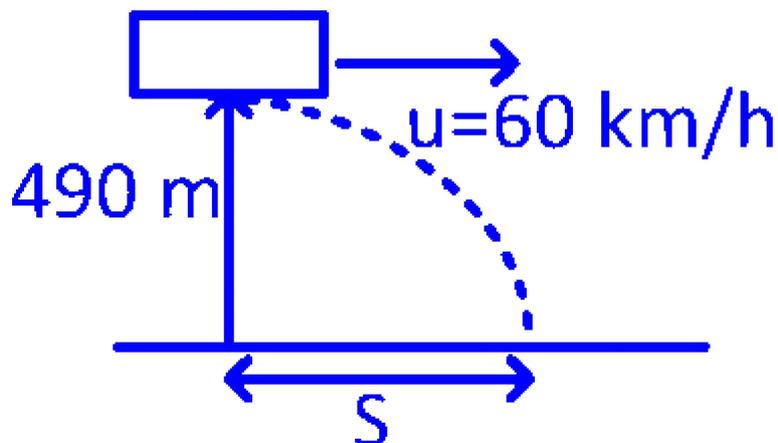
Answer: B

Solution:

Given,

$$\begin{aligned}\text{Initial speed of plane} &= 60\text{ km/h} \\ &= \frac{50}{3}\text{ m/s}\end{aligned}$$

Vertical height $\mp 490\text{ m}$ Horizontal distance



...(i)



$$s = u \times t \quad (s = ut + \frac{1}{2}at^2)$$
$$(a = 0) \quad (s)$$

For vertical component of motion,

$$u = 0$$

using equation of motion,

$$s = ut + \frac{1}{2}at^2 (a = g)$$

$$t = \sqrt{\frac{2s}{g}} \Rightarrow t = \sqrt{\frac{2 \times 490}{9.8}}$$

$$t = 10 \text{ s}$$

Put this in Eq. (i)

$$s = \frac{50}{3} \times 10$$

$$s = \frac{500}{3} \text{ m}$$

